Compact Stars in a SU(3) Quark-Meson model

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2 Theoretical framework





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Hypothesis of a Strange Quark Star



Strange Quark Matter Hypothesis

Hypothesis (Bodmer('71) – Terezawa('79) – Witten('84)): Three flavour beta-stable quark matter is more bound than 56 Fe



Starting with a mixture of up and down quarks, the weak process $u + d \rightarrow u + s$ allows to decrease E/A (a new Fermi sphere opens) to values smaller than 930 MeV.

Relation to the QCD Phase Diagram



- · Compact star matter at small temperature and high density
- · Early universe at zero density and high temperature
- Probed by heavy-ion collisions at LHC, RHIC, GSI, NICA, ...
- \Rightarrow At sufficiently high density the nucleonic matter will make a transition to the quark matter state.

Transition of Nuclear Matter to Quark Matter

At sufficiently high density the nucleonic matter will make a transition to the quark matter state.



Investigate the transition to quark matter at T = 0 in an effective model of QCD: A. Zacchi, RS, J. Schaffner-Bielich; Phys. Rev. D 92 (2015) 4, 045022

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Ingredients of the Quark-Meson model

$$\mathcal{L}_{\text{QM}} = \bar{q} \left[i \gamma_{\mu} \left(\partial^{\mu} + \mu_{f} \, \delta^{\mu 0} \right) - g \, \frac{\lambda_{a}}{2} \left(\sigma_{a} + i \gamma_{5} \pi_{a} \right) - g_{v} \, \gamma^{\mu} V_{\mu} \right] q \\ + \frac{1}{2} \left(\partial_{\mu} \sigma_{a} \partial^{\mu} \sigma_{a} + \partial_{\mu} \pi_{a} \partial^{\mu} \pi_{a} \right) - U \left(\sigma_{1}, \sigma_{s} \right) - U_{v} \left(\omega, \rho, \phi \right) - B$$

Ingredients:

- constituent quarks
- scalar and pseudoscalar mesons $\langle ar{q}q
 angle$
 - → generation of constituent quark masses by meson exchange (Yukawa coupling): $m_f = g\sigma_f$
- repulsive interaction by vector meson exchange
- vacuum pressure: bag constant B^{1/4}
- → scalar fields: order parameters for chiral symmetry breaking

Doing calculations in the QM model

- Mean-field approximation: $\mathcal{L} \rightsquigarrow \mathcal{Z} \rightsquigarrow \Omega$ effective potential
- $\Omega(\sigma_1, \sigma_s, \omega, \rho, \phi; \mu_f, \mu_e) = B + U(\sigma_1, \sigma_s) + U_v(\omega, \rho, \phi) + \Omega_{q\bar{q}}(\sigma_1, \sigma_s, \omega, \rho, \phi; \mu_f) + \Omega_e(\mu_e)$
- equations of motion: $\partial \Omega / \partial \varphi_i = 0$, $\varphi_i \in \{\sigma_1, \sigma_s, \omega, \rho, \phi\}$ Charge neutrality: $n_Q = 0$

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- · Thermodynamic relations:

$$p = -\Omega$$
, $s = -\frac{\partial \Omega}{\partial T} = 0$, $n_f = -\frac{\partial \Omega}{\partial \mu_f}$, $\epsilon = \Omega + Ts + \sum_{f=u,d,s} \mu_f n_f$

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• Parameters:

 σ -meson mass: $m_{\sigma} \simeq 400 - 1000 \,\text{MeV}$ constituent quark mass: $m_{q} \simeq 100 - 400 \,\text{MeV}$ Vector coupling: $g_{\omega} \simeq 1 - 7$ Vacuum pressure: $B^{1/4} \simeq 0 - 140 \,\text{MeV}$

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Chiral Phase Transition in the QM model

Restoration of chiral symmetry with increasing density in the light and strange quark sector.



A. Zacchi, RS, J. Schaffner-Bielich; Phys. Rev. D 92 (2015) 4, 045022

\Rightarrow Depending on the parameters the transition is smooth or discontinuous.

Equation of state and mass-radius relation

Calculate the equation of state within the model and solve the TOV equations to gain the mass-radius relation.



 $m_{\rm q} = 300 \,{\rm MeV}, \, m_{\sigma} = 600 \,{\rm MeV}, \, B^{1/4} = 120 \,{\rm MeV}$

⇒ Depending on the undetermined parameters, maximum masses of two or more solar masses are possible.

Stability conditions



A. Zacchi, RS, J. Schaffner-Bielich; Phys. Rev. D 92 (2015) 4, 045022

⇒ Observed pulsar masses and stability conditions on nuclear and quark matter can constrain the parameter space of QCD model.

Further Ingredients to the Model

$$\Omega_{q\bar{q}}\left(\sigma_{1},\sigma_{s},\omega,\rho,\phi;\mu_{f}\right) = \Omega_{q\bar{q}}^{\text{th}}\left(\sigma_{1},\sigma_{s},\omega,\rho,\phi;\mu_{f}\right) + \Omega_{q\bar{q}}^{\text{vac}}\left(\sigma_{1},\sigma_{s}\right)$$



 \Rightarrow Softening of EoS \rightarrow Further restrictions on parameter space.

Considering a nuclear crust

EoS of inner and outer nuclear crust

J. W. Negele, D. Vautherin, Nucl. Phys. A 207 (1973) 298–320 S. B. Ruester, M. Hempel, J. Schaffner-Bielich, Phys. Rev. C 73 (2006), 035804



 \Rightarrow When vacuum fluctuations are included much less impact of considering nuclear crust.

Conclusions

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- Describing restoration of chiral symmetry with increasing density at T=0 with the Quark-Meson model
- Application to the 2+1 flavour quark matter equation of state for compact stars
- Depending on unknown parameters maximum masses of 2 M_{\odot} or more can be obtained
- Large pulsar masses together with stability conditions constrain parameter space significantly
 → Impact of pulsar measurements on QCD models
- The more elaborated the model, the tighter the parameter constraints



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Thank You for your attention!

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Introduction	Theoretical framework	Results	Conclusions
Backup			

Selfbound Quark Stars vs. Ordinary Neutron Stars



Quark Stars

- Mass-radius relation starts at the origin (ignoring a possible crust)
- Arbitrary small masses and radii possible
- Selfbound: vanishing pressure at a finite energy density

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Neutron Stars

- Mass-radius relation starts at large radii
- Minimum neutron star mass: $M \sim 0.1 M_{\odot}$ with $R \sim 200 \text{ km}$
- Bound by gravity, finite pressure for all energy densities

Constraints from Astrophysical Observations

Reliable constraints on the radius from observations?



 $6 \text{ km} \lesssim R \lesssim 15 \text{ km}$ at 68% confidence ...

Constraints from Astrophysical Observations

Reliable constraints on the radius from observations?



Combinded baysian analysis assuming a constant radius for $M \ge 0.5 M_{\odot} \dots$

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Sebastien Guillot: Observations of Neutron Stars; Compstar School Septembre 2015